

Introduzione:

CRITERI DI RESISTENZA STATICA

- Dato un generico stato di sforzo, come possiamo capire se è critico o meno per un componente?
- Abbiamo bisogno di uno "strumento" che ci permetta di ~~quantificare~~ quantificare la criticità dello stato di sforzo rispetto alle caratteristiche del materiale che si vuole adottare.

Equazione di verifica:

$$\sigma^* \leq \sigma_{amm} = \frac{\sigma_{lim}}{\eta}$$

Proprietà del materiale

←

← Coefficiente di sicurezza

Sforno di componente o sforno equivalente

Il calcolo dello sforno equivalente viene svolto attraverso l'utilizzo di un criterio di resistenza ~~proprio~~ ~~proprio~~ che dipende dal materiale utilizzato:

MATERIALI DUTILI

↳ Criterio di Guest-Tresca

$$\tau_{max} \leq \tau_{amm} = \frac{\tau_{lim}}{\eta} \quad \text{dove} \quad \tau_{lim} = \tau_{sn} = \frac{\sigma_{sn}}{2}$$

$$\tau_{max} = \frac{\sigma_I - \sigma_{III}}{2} \leq \tau_{amm} = \frac{\sigma_{sn}}{2} \frac{1}{\eta}$$

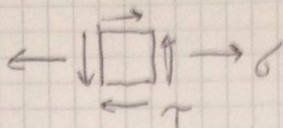
$$\Rightarrow \sigma_{GT}^* = \sigma_I - \sigma_{III} \leq \sigma_{amm} = \frac{\sigma_{sn}}{\eta}$$

Scritta anche come: $\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min}$

↳ Criterio di Von Mises

$$\sigma_{VM}^* = \sqrt{\sigma_I^2 + \sigma_{II}^2 + \sigma_{III}^2 - \sigma_I \sigma_{II} - \sigma_{II} \sigma_{III} - \sigma_{III} \sigma_I}$$

Caso Lipio



Formule semplificate:

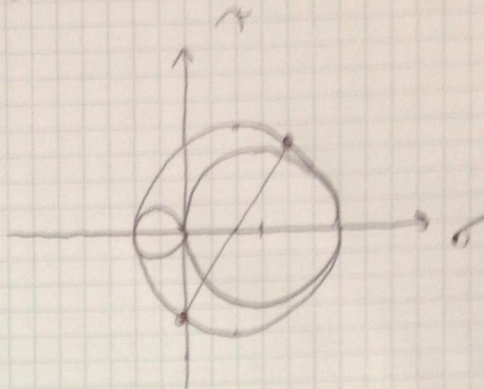
$$\sigma_I = \frac{\sigma}{2} + \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2}$$

$$\sigma_{II} = 0$$

$$\sigma_{III} = \frac{\sigma}{2} - \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2}$$

$$\Rightarrow \sigma_{GT}^* = \sigma_I - \sigma_{II} = \sqrt{\sigma^2 + 4\tau^2}$$

$$\sigma_{VM}^* = \sqrt{\sigma^2 + 3\tau^2}$$



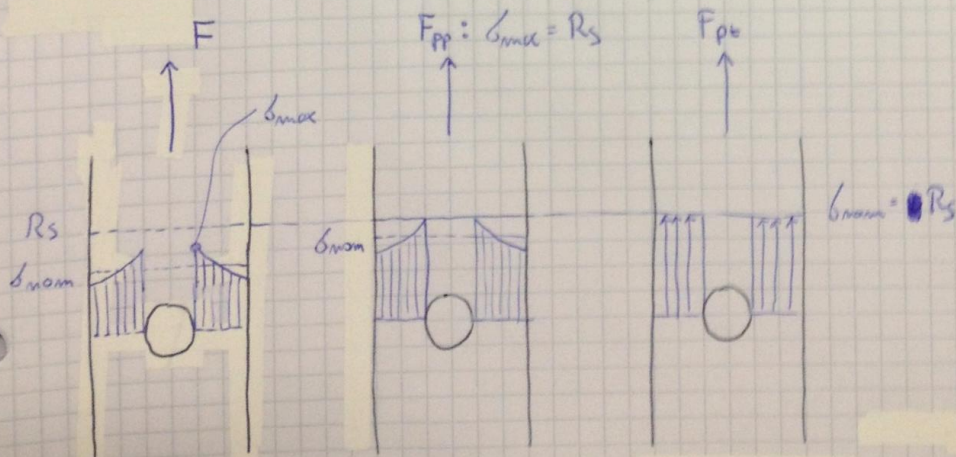
MATERIALI FRAGILI

↳ Galileo, Rankine, Navier

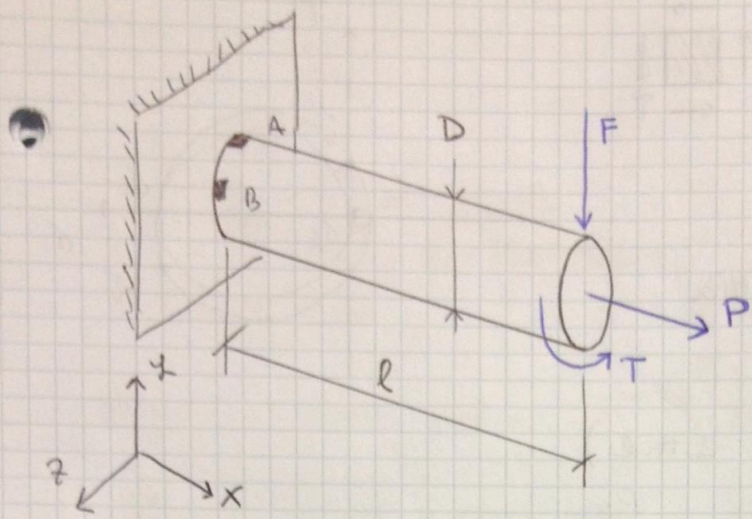
Il cedimento si verifica quando uno degli sforzi principali diventa uguale allo sforzo di rottura a trazione σ_m^t (R_m^t) o a compressione (σ_m^c o σ_m^c)

$$\sigma_{GRV}^* = \sigma_I \leq \frac{R_m^t}{\gamma}$$

$$\sigma_{GRV}^* = \sigma_{III} \geq \frac{R_m^c}{\gamma}$$

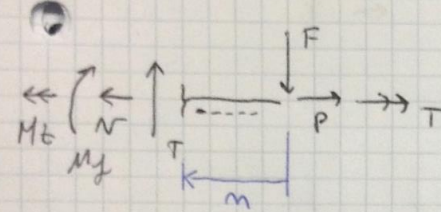
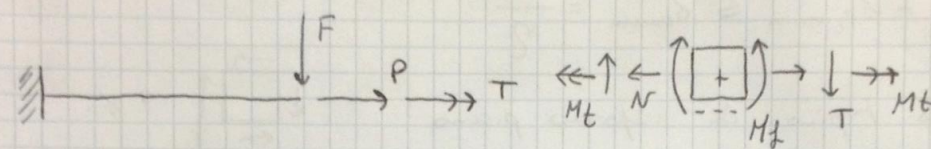


Spiega che
 σ_{nom}
 si trovano
 nella sezione
 "minore"

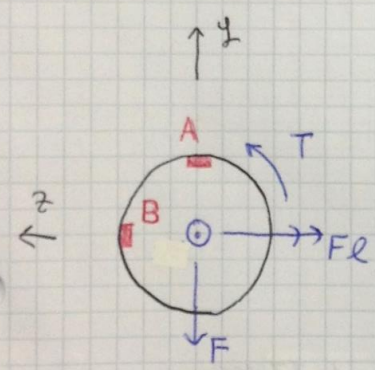
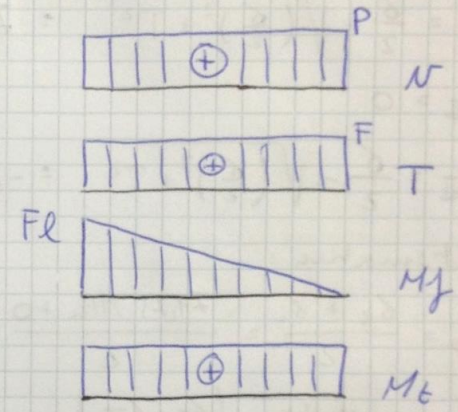


$D = 20 \text{ mm}$
 $l = 100 \text{ mm}$
 $F = 550 \text{ N}$
 $P = 8000 \text{ N}$
 $T = 30 \text{ Nm}$

Materiale: acciaio Fe430
 $R_m = 430 \text{ MPa}$
 $R_s = 275 \text{ MPa}$



$N = P$
 $T = F$
 $M_z = -Fm$
 $M_t = T$



Punto A: $\sigma_{x,N} = \frac{P}{A} = \frac{P}{\frac{\pi D^2}{4}} = \frac{8000 \text{ N}}{\frac{\pi 20^2 \text{ mm}^2}{4}} = 25,47 \text{ MPa}$
 $\sigma_{x,Mz} = \frac{M_z D/2}{J} = \frac{M_z D/2}{\frac{\pi D^4}{64}} = 70 \text{ MPa}$
 $\tau_{xz} = \frac{T D/2}{J_p} = \frac{T D/2}{\frac{\pi D^4}{32}} = \frac{30 \text{ N}\cdot\text{m} \cdot 10^3 \frac{\text{mm}}{\text{m}} \cdot \frac{20 \text{ mm}}{2}}{\frac{\pi 20^4 \text{ mm}^4}{32}} = 19,1 \text{ MPa}$
 $\sigma_{x,tot} = 95,47 \text{ MPa}$

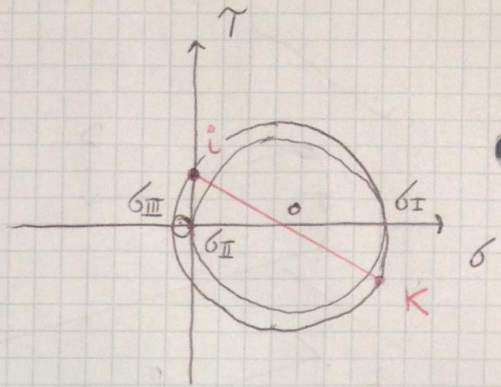
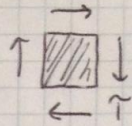
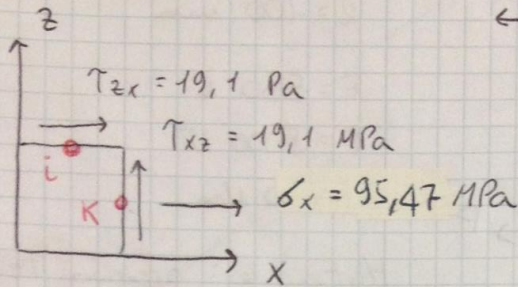
Punto B: $\sigma_{x,N} = 25,47 \text{ MPa}$

$\tau_{x_{shear}} = 19,1 \text{ MPa}$

$\tau_{x_{shear}} = \frac{4}{3} \frac{F}{A} = \frac{4}{3} \frac{550 \text{ N}}{\frac{\pi D^2}{4}} = 2,33 \text{ MPa}$

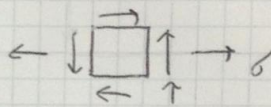
$\tau_{xy} = 21,43 \text{ MPa}$

Punto A:



Guest-Tresca (materiali duttili)

$$\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min} \leq \sigma_{amm} = \frac{R_s}{\eta}$$

Per questo caso tipico di sforzo piano: 

$$\sigma_I = \frac{\sigma}{2} + \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2} = 99,15 \text{ MPa}$$

$$\sigma_{II} = 0$$

$$\sigma_{III} = \frac{\sigma}{2} - \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2} = -4,77$$

Alternativa:

$$\sigma_0 = \frac{\sigma_k + \sigma_i}{2} = \frac{95,47 \text{ MPa} + 0}{2} = 47,74 \text{ MPa}$$

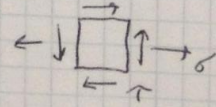
Raggio cerchio ($\sigma_I - \sigma_{III}$):

$$\overline{OK} = \sqrt{\tau_k^2 + (\sigma_{II} - \sigma_0)^2} = 51,41 \text{ MPa}$$

$$\sigma_I = \sigma_0 + \overline{OK} = 99,15 \text{ MPa} \quad \sigma_{III} = \sigma_0 - \overline{OK} = -3,67 \text{ MPa}$$

$$\sigma_{GT}^* = \sigma_I - \sigma_{III} = 99,15 \text{ MPa} - (-3,67) \text{ MPa} = 102,8 \text{ MPa}$$

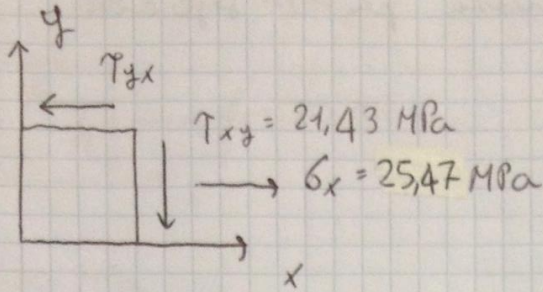
$$\sigma_{GT}^* \leq \sigma_{amm} = \frac{R_s}{\eta_{GT}} \rightarrow \eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = \frac{275 \text{ MPa}}{102,8 \text{ MPa}} = 2,68 > \eta_{duttile} = 1,5$$

Alternativa calcolo σ_{GT}^* : caso di sforzo piano 

$$\sigma_{GT}^* = \sqrt{\sigma^2 + 4\tau^2} = 102,83 \text{ MPa}$$

$$\sigma_{VM}^* = \sqrt{\sigma^2 + 3\tau^2} = 101,04 \text{ MPa} \quad \sigma_{VM}^* \leq \frac{R_s}{\eta_{VM}} \rightarrow \eta_{VM} = 2,72 > \eta_{duttile} = 1,5$$

Punto B:



Stato di sforzo piano :

$$\sigma_{GT}^* = \sqrt{\sigma^2 + 4\tau^2} = 49,85 \text{ MPa} \leq \frac{R_s}{\nu_{GT}} \rightarrow \nu_{GT} = 5,52$$

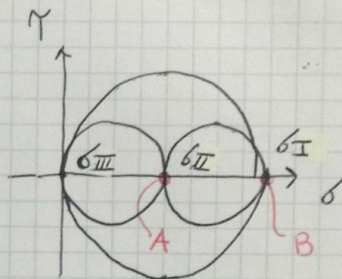
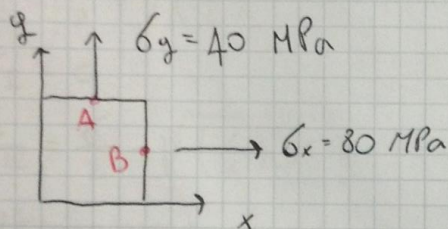
$$\sigma_{VM}^* = \sqrt{\sigma^2 + 3\tau^2} = 45 \text{ MPa} \leq \frac{R_s}{\nu_{VM}} \rightarrow \nu_{VM} = 6,11$$

Barrile di acciaio duttile con snamento $R_s = 345 \text{ MPa}$.
 Calcolare i coefficienti di sicurezza per i seguenti stati di sforzo:

- 1) $\sigma_x = 80 \text{ MPa}$; $\sigma_y = 40 \text{ MPa}$
- 2) $\sigma_x = 80 \text{ MPa}$; $\sigma_y = -60 \text{ MPa}$
- 3) $\sigma_x = -40 \text{ MPa}$; $\sigma_y = -70 \text{ MPa}$; $\tau_{xy} = -35 \text{ MPa}$
- 4) $\sigma_x = 80 \text{ MPa}$; $\sigma_y = 25 \text{ MPa}$; $\tau_{xy} = 10 \text{ MPa}$

Ripetere i calcoli con una ghisa con $R_{m,t} = 200 \text{ MPa}$ e $R_{m,c} = -690 \text{ MPa}$

Es. 1



$$\begin{aligned}\sigma_I &= 80 \text{ MPa} \\ \sigma_{II} &= 40 \text{ MPa} \\ \sigma_{III} &= 0 \text{ MPa}\end{aligned}$$

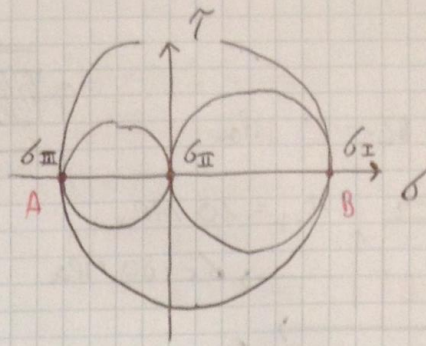
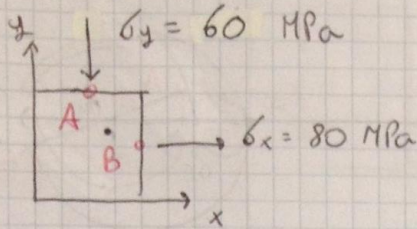
Cavst-Tresca: $\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min} = \sigma_I - \sigma_{III} = 80 \text{ MPa}$

$$\sigma_{GT}^* = 80 \text{ MPa} \leq \sigma_{amm} = \frac{R_s}{\eta_{GT}} \quad \eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = \frac{345 \text{ MPa}}{80 \text{ MPa}} = 4,31$$

Von Mises:
$$\begin{aligned}\sigma_{VM}^* &= \sqrt{\sigma_I^2 + \sigma_{II}^2 + \sigma_{III}^2 - \sigma_I \sigma_{II} - \sigma_{II} \sigma_{III} - \sigma_{III} \sigma_I} = \\ &= \sqrt{\sigma_I^2 + \sigma_{II}^2 - \sigma_I \sigma_{II}} = 69,3 \text{ MPa}\end{aligned}$$

$$\sigma_{VM}^* = 69,3 \text{ MPa} \leq \sigma_{amm} = \frac{R_s}{\eta_{VM}} \rightarrow \eta_{VM} = \frac{R_s}{\sigma_{VM}^*} = 4,98$$

Es. 2



$$\sigma_I = 80 \text{ MPa}$$

$$\sigma_{II} = 0 \text{ MPa}$$

$$\sigma_{III} = -60 \text{ MPa}$$

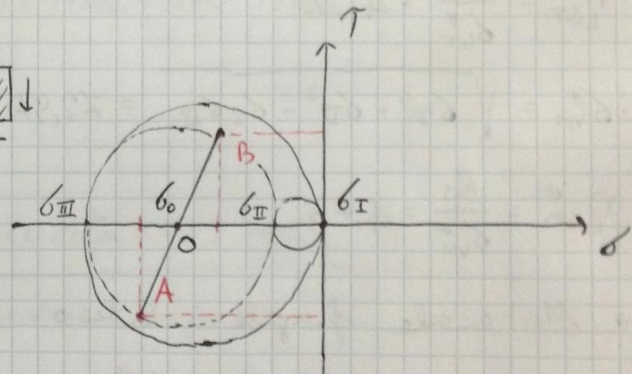
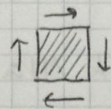
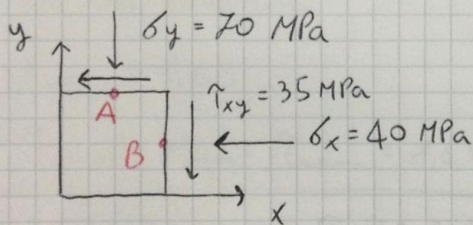
$$\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min} = 80 \text{ MPa} - (-60 \text{ MPa}) = 140 \text{ MPa}$$

$$\sigma_{GT}^* = \frac{R_s}{\eta_{GT}} \rightarrow \eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = 2,46$$

$$\sigma_{VM}^* = \sqrt{\sigma_I^2 + \sigma_{II}^2 + \sigma_{III}^2 - \sigma_I \sigma_{II} - \sigma_{II} \sigma_{III} - \sigma_{III} \sigma_I} = 121,7 \text{ MPa}$$

$$\eta_{VM} = \frac{R_s}{\sigma_{VM}^*} = 2,83$$

Es. 3



$$\sigma_0 = \frac{\sigma_B + \sigma_A}{2} = \frac{-40 - 70}{2} = -55 \text{ MPa}$$

$$\overline{OB} = \sqrt{(\sigma_B - \sigma_0)^2 + \tau_B^2} = 38,08 \text{ MPa}$$

$$\sigma_I = 0; \quad \sigma_{II} = \sigma_0 + \overline{OB} = -16,92 \text{ MPa}; \quad \sigma_{III} = \sigma_0 - \overline{OB} = -93,08 \text{ MPa}$$

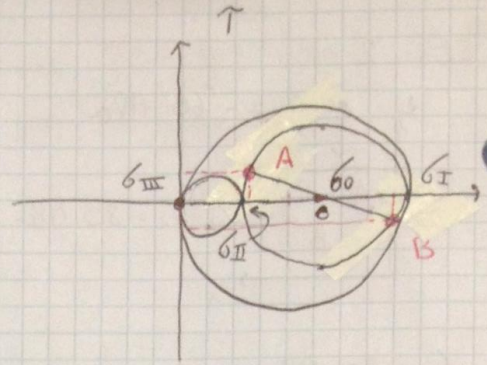
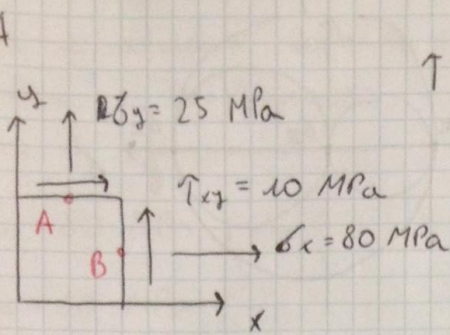
$$\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min} = 0 - (-93,08) \text{ MPa} = 93,08 \text{ MPa}$$

$$\eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = 3,71$$

$$\sigma_{VM}^* = \sqrt{\sigma_I^2 + \sigma_{II}^2 + \sigma_{III}^2 - \sigma_I \sigma_{II} - \sigma_{II} \sigma_{III} - \sigma_{III} \sigma_I} = 85,88 \text{ MPa}$$

$$\eta_{VM} = \frac{R_s}{\sigma_{VM}^*} = 4,02$$

Es. 4



$$\sigma_0 = \frac{\sigma_A + \sigma_B}{2} = \frac{(25 + 80) \text{ MPa}}{2} = 52,5 \text{ MPa}$$

$$\overline{OB} = \sqrt{(\sigma_B - \sigma_0)^2 + \tau_B^2} = 29,26 \text{ MPa}$$

$$\sigma_I = \sigma_0 + \overline{OB} = 81,76 \text{ MPa}$$

$$\sigma_{II} = \sigma_0 - \overline{OB} = 23,24 \text{ MPa}$$

$$\sigma_{III} = 0$$

$$\sigma_{GT}^* = \sigma_{p, \max} - \sigma_{p, \min} = 81,76 \text{ MPa} - 0 \text{ MPa} = 81,76 \text{ MPa}$$

$$\eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = 4,22$$

$$\sigma_{vm}^* = \sqrt{\sigma_I^2 + \sigma_{II}^2 - \sigma_I \sigma_{II}} = 72,97 \text{ MPa}$$

$$\eta_{vm}^* = \frac{R_s}{\sigma_{vm}^*} = 4,73$$

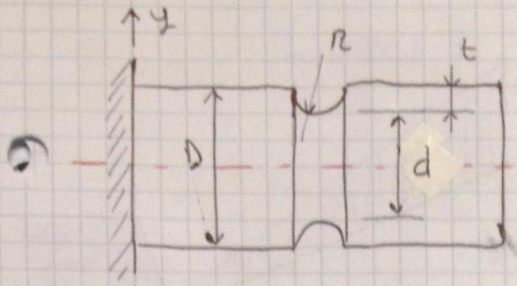
→ Materiale fragile: criterio di Galileo, Rankine, Navier

Es. 1: $\sigma_I = 80 \text{ MPa}$ $\sigma_{GT, t}^* \leq \sigma_{lim, \max} = \frac{R_{m, t}}{\eta_{GRV, t}}$ $\eta_{GRV, t} = \frac{R_{m, t}}{\sigma_{GT, t}^*} = 2,5$
 $\sigma_{III} = 0 \text{ MPa}$
 $2,5 < 3,0$! Non verificato (il 2° $\eta \rightarrow \infty$)

Es. 2: $\sigma_I = 80 \text{ MPa}$ $\eta_{GRV} = \frac{R_{m, t}}{\sigma_{GRV, t}^*} = 2,5 < 3,0$ non verificato!
 $\sigma_{II} = -60 \text{ MPa}$

Es. 3: $\sigma_I = 0 \text{ MPa}$ $\eta_{GRV} = \frac{|R_{m, c}|}{\sigma_{GRV, c}^*} = 2,42$ (il 1° $\eta \rightarrow \infty$)
 $\sigma_{III} = -93 \text{ MPa}$

Es. 4: $\sigma_I = 81,76 \text{ MPa}$ $\eta_{GRV} = \frac{R_{m, t}}{\sigma_{GRV, t}^*} = 2,46 < 3$ Non verificato
 $\sigma_{III} = 0 \text{ MPa}$
 (il 2° $\eta \rightarrow \infty$)



$$t = 10,5 \text{ mm}$$

$$R = 7 \text{ mm}$$

$$D = 70 \text{ mm}$$

$$M = 1 \text{ kNm}$$

$$T = 2,5 \text{ kNm}$$

$$\sigma_{x, \text{nom}} = \frac{M \cdot d/2}{J} = \frac{M \cdot d/2}{\frac{\pi d^4}{64}} = 86,58 \text{ MPa}$$

• Trovare stato
di sforzo nelle
gole dell'intaglio

$$d = D - 2t = 49 \text{ mm}$$

$$\tau_{\text{nom}} = \frac{T \cdot d/2}{J_p} = \frac{T \cdot d/2}{\frac{\pi d^4}{32}} = 108,22 \text{ MPa}$$

• Per la flessione:

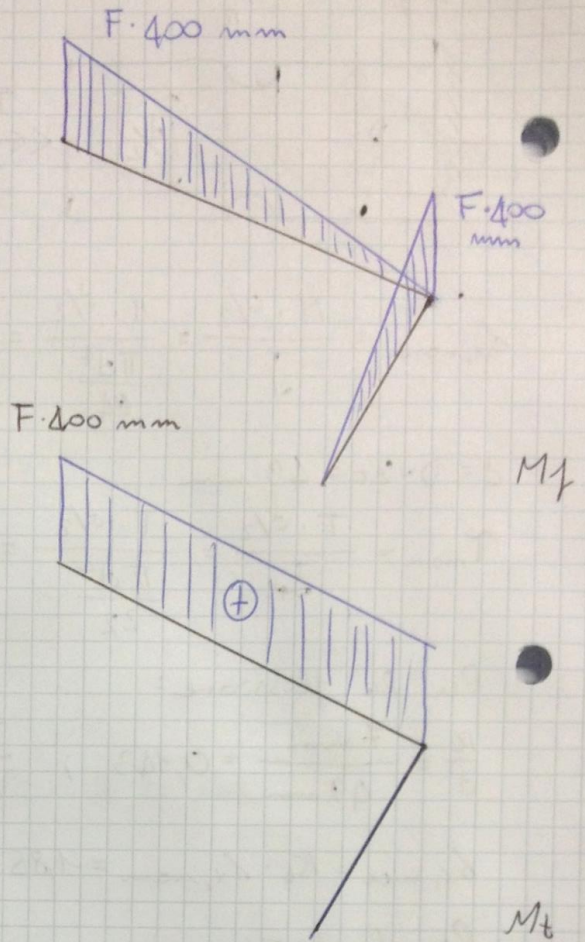
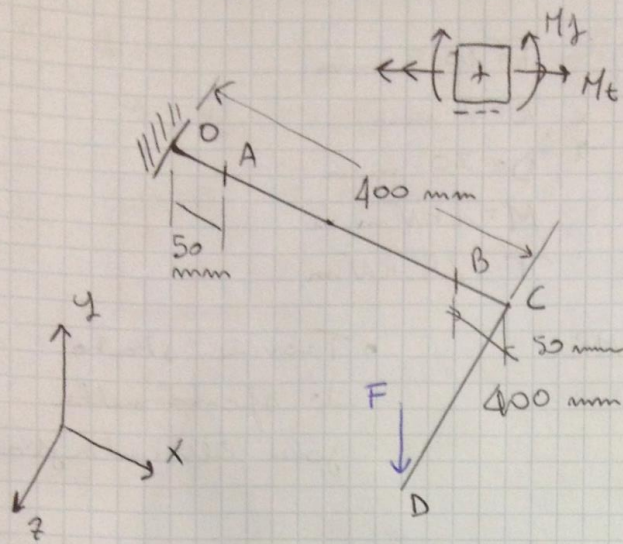
$$\frac{R}{d} = \frac{7 \text{ mm}}{49 \text{ mm}} = 0,143 ; \quad \frac{D}{d} = 1,43 \rightarrow K_{t(M)} = 1,85$$

$$\sigma_{x, \text{max}} = K_t \cdot \sigma_{x, \text{nom}} = 1,85 \cdot 86,58 \text{ MPa} = 160 \text{ MPa}$$

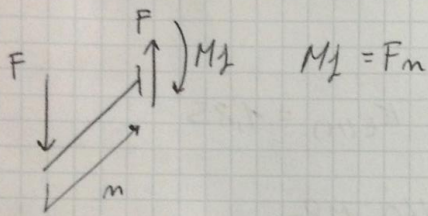
Per la torsione:

$$K_{t(T)} = 1,43$$

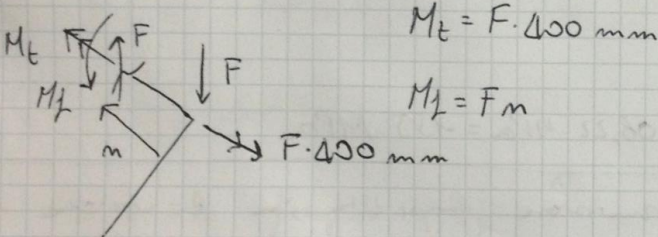
$$\tau_{\text{max}} = K_{t(T)} \cdot \tau_{\text{nom}} = 1,43 \cdot 108,22 \text{ MPa} = 155 \text{ MPa}$$



Tramo DC:



Tramo OC:



Nel punto A, dove c'è il cambio di diametro:

$$M_t = F \cdot 400 \text{ mm}$$

$$M_z = F \cdot 350 \text{ mm}$$

Spessi nominali (si calcolano sul diametro minore):

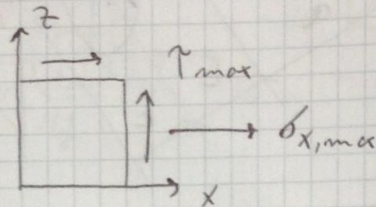
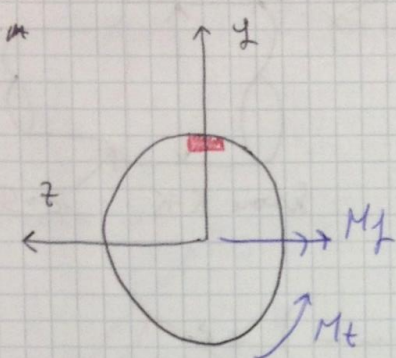
$$\sigma_{x, \text{nom}} = \frac{M_z \cdot d/2}{\frac{\pi d^4}{64}} = F \cdot 0,22816 \text{ MPa}$$

$$\tau_{\text{nom}} = \frac{M_t \cdot d/2}{J_p} = \frac{M_t \cdot d/2}{\frac{\pi d^4}{32}} = F \cdot 0,1304 \text{ MPa}$$

$$\frac{R}{d} = 0,12 \quad ; \quad \frac{D}{d} = 1,6 \quad ; \quad K_{t,M_t} = 1,7 \quad ; \quad K_{t,M_t} = 1,35$$

$$\sigma_{x,max} = \sigma_{nom} \cdot K_t = F \cdot 0,3879 \text{ MPa}$$

$$\tau_{max} = K_{t,M_t} \cdot \tau_{nom} = F \cdot 0,17604 \text{ MPa}$$



Ho usato $\sigma_{x,max}$ e τ_{max}

$$\sigma_{VM}^* = \sqrt{\sigma^2 + 3\tau^2} = F \cdot 0,4934 \text{ MPa} = R_s = 460 \text{ MPa}$$

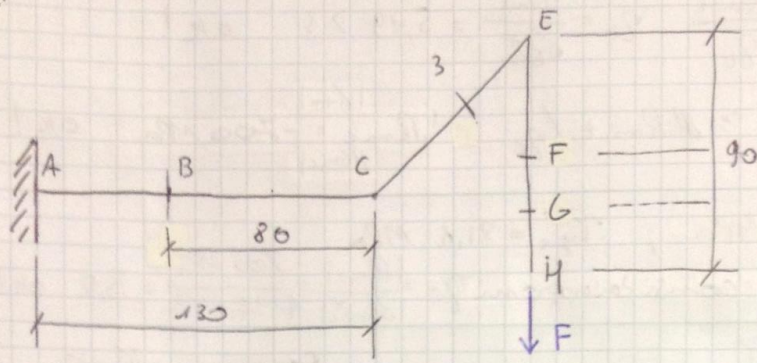
Significa che siamo a inizio plasticizzazione locale

$$\Rightarrow F = 932 \text{ N} \quad (\text{Von Mises})$$

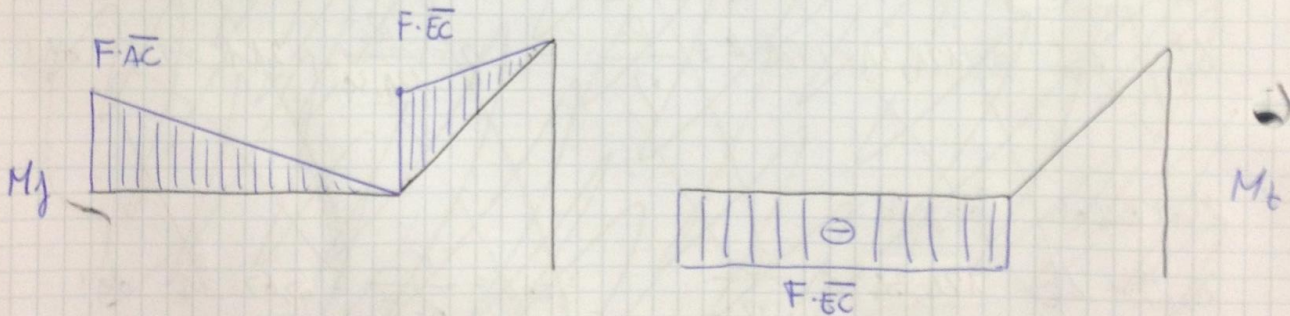
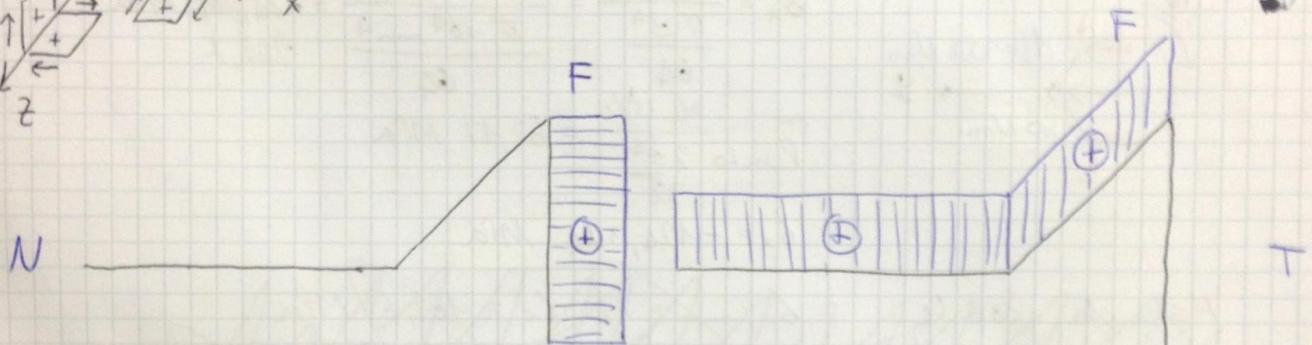
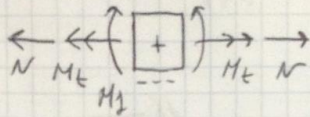
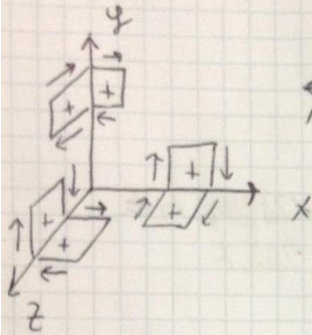
$$\sigma_{GT}^* = \sqrt{\sigma^2 + 4\tau^2} = F \cdot 0,5239 \text{ MPa} = R_s = 460 \text{ MPa}$$

$$\Rightarrow F = 878 \text{ N} \quad (\text{Guest-Trecca})$$

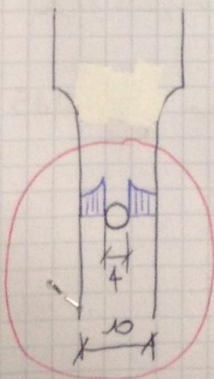
Esercizio leva



- Azioni interne
- Dati 2 materiali (Fe410 e GG25)
- Calcolare F_{max} per il tratto rettangolare
- Calcolare σ_{max}



Tratto EH: FORO



$$\sigma_{nom} = \frac{F}{A_{nom}} = \frac{F}{(10-4)6 \text{ mm}^2} = \frac{F}{36 \text{ mm}^2}$$

$$K_t \rightarrow \frac{d}{H} = \frac{4 \text{ mm}}{10 \text{ mm}} = 0,4 \rightarrow K_t = 2,25$$

Prima plasticizzazione (Materiale duttile Fe410):

$$\sigma_{max} = R_s = K_t \cdot \sigma_{nom} \rightarrow \sigma_{nom} = \frac{R_s}{K_t} = \frac{230 \text{ MPa}}{2,25} = 102 \text{ MPa}$$

$$\sigma_{nom} = \frac{F_{lim,pp}}{36 \text{ mm}^2} \rightarrow F_{lim,pp} = \sigma_{nom} \cdot 36 \text{ mm}^2 = 3680 \text{ N}$$

Forza di prima plasticizzazione sul fuso con materiale duttile: $F = 3680 \text{ N}$

Forza di plasticizzazione totale: tutta la sezione nominale del fuso ha sforzi $= R_s$

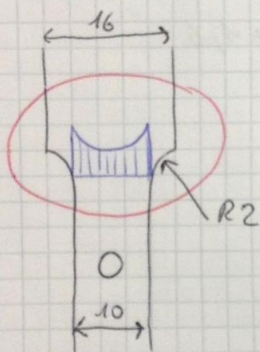
$$\sigma_{nom} = R_s \rightarrow \sigma_{nom} = \frac{F_{lim,pt}}{36 \text{ mm}^2} = R_s \rightarrow F_{lim,pt} = R_s \cdot 36 \text{ mm}^2 = 8280 \text{ N}$$

Se utilizziamo materiale fragile:

$$R_m = 250 \text{ MPa}$$

$$\sigma_{max} = R_m = K_t \cdot \sigma_{nom} = K_t \cdot \frac{F_{lim}}{36 \text{ mm}^2} \Rightarrow F_{lim} = \frac{R_m}{K_t} \cdot 36 \text{ mm}^2 = 4000 \text{ N}$$

Tracce EH: INTAGLIO



$$\sigma_{nom} = \frac{F}{A} = \frac{F}{10 \text{ mm} \cdot 6 \text{ mm}} = \frac{F}{60 \text{ mm}^2} = \frac{F}{A}$$

$$F = \sigma_{nom} \cdot A$$

Materiale duttile (Fe410):

Forza di 1^a plasticizzazione: Condizione $\sigma_{max} = R_s$

$$\sigma_{max} = K_t \cdot \sigma_{nom} \quad K_t = 1,75$$

$$\sigma_{max} = 1,75 \cdot \sigma_{nom} = R_s$$

$$r/h = 0,2 \quad H/h = 1,6$$

$$K_t \cdot \frac{F_{lim,pp}}{A} = R_s \quad F_{lim,pp} = \frac{A \cdot R_s}{K_t} = \frac{60 \text{ mm}^2 \cdot 230 \text{ MPa}}{1,75} = 7895 \text{ N}$$

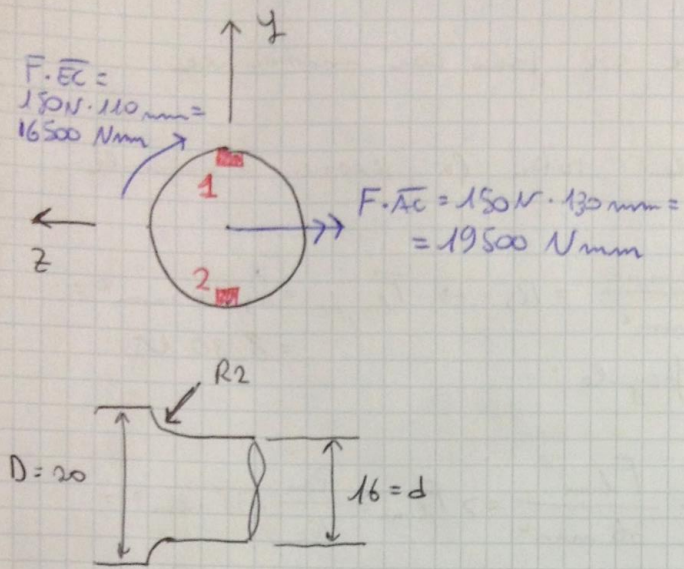
Forza di plasticizzazione totale: Condizione: tutta la sezione R_s

$$F_{lim,pt} = R_s \cdot A = 230 \text{ MPa} \cdot 60 \text{ mm}^2 = 13800 \text{ N}$$

Materiale fragile (GG25):

$$\sigma_{max} = K_t \cdot \sigma_{nom} = R_m \quad K_t \cdot \frac{F_{lim}}{A} = R_m \quad F_{lim} = \frac{A \cdot R_m}{K_t} = 8571 \text{ N}$$

Verifica solo nel punto A:



Punto 1:

$$\sigma_x = \frac{M_f \cdot d/2}{J} = \frac{M_f \cdot d/2}{\frac{\pi d^4}{64}} = 48,5 \text{ MPa}$$

$$\tau_{xz} = \frac{M_t \cdot d/2}{\frac{\pi d^4}{32}} = -20,52 \text{ MPa}$$

~~Punto 2:~~

$$\sigma_x = -48,5 \text{ MPa}$$

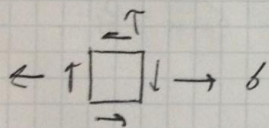
$$\tau_{xz} = 20,52 \text{ MPa}$$

$$M_f: r/d = \frac{2}{16} = 0,125 ; \quad \frac{D}{d} = \frac{20}{16} = 1,25 \quad K_{t(M_f)} = 1,6$$

$$M_t: r/d = 0,125 ; \quad \frac{d}{D} = 0,8 \quad K_t = 1,28$$

Punto 1: ~~σ_x~~ $\sigma_{x,max} = K_{t(M_f)} \cdot \sigma_x = 77,6 \text{ MPa}$

$$\tau_{xz} = K_{t(M_t)} \cdot \tau_{xz} = -26,27 \text{ MPa}$$



$$\sigma_I = \frac{\sigma}{2} + \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2} = 85,66 \text{ MPa}$$

$$\sigma_{II} = 0$$

Materiale
 Duttile:

$$\sigma_{III} = \frac{\sigma}{2} - \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2} = -8 \text{ MPa}$$

$$\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min} = 85,66 \text{ MPa} - (-8) \text{ MPa} = 93,72 \text{ MPa}$$

$$\sigma_{GT}^* \leq \sigma_{amm} = \frac{R_s}{\eta_{GT}} \Rightarrow \eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = \frac{230 \text{ MPa}}{93,72 \text{ MPa}} = 2,45 \quad (\text{prima plasticizzazione})$$

Sulla plasticizzazione totale:

$$\sigma_I = 56 \text{ MPa} ; \quad \sigma_{II} = 0 ; \quad \sigma_{III} = -7,52 \text{ MPa} \quad (\text{calcolati con gli stress nominali})$$

$$\sigma_{GT}^* = 63,51 \text{ MPa}$$

$$\eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = 3,62 \quad (\text{plasticizzazione totale})$$

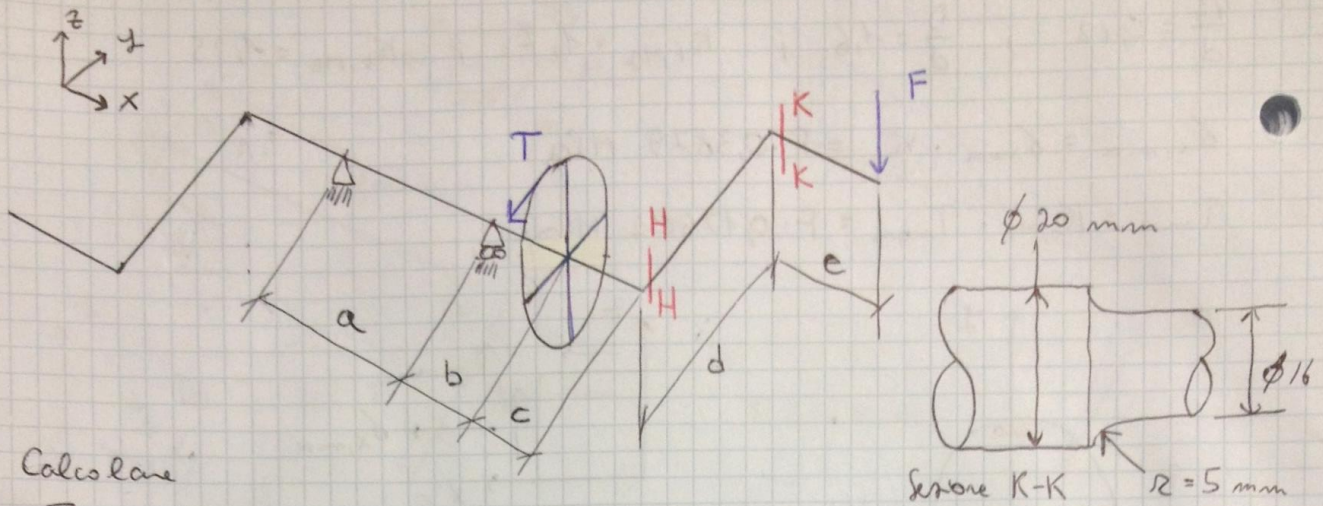
(Si potevamo usare anche le formule semplificate)

$$\sigma_{GT}^* = \sqrt{\sigma^2 + 4\tau^2}$$

Materiale fragile:

$$\sigma_{GRV}^* = \sigma_{p,max} = \sigma_I \leq R_m / \eta_{GRV}$$

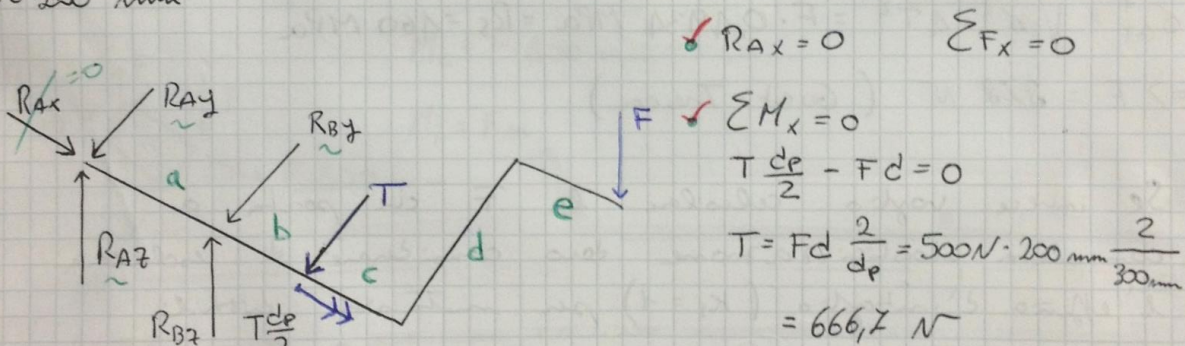
$$\eta_{GRV} = \frac{R_m}{\sigma_I} = \frac{250 \text{ MPa}}{85,66 \text{ MPa}} = 2,93$$



Calcolare

- o Forza T esercitata sulla catena
 - o Diagramma delle azioni interne
 - o Calcolo sforzi principali in H-H ($\phi = 20 \text{ mm}$) e effettuare verifica di resistenza statica con materiale
- A: $R_s = 300 \text{ MPa}$; $R_m = 500 \text{ MPa}$, B: $R_m = 200 \text{ MPa}$

$a = 50 \text{ mm}$ $e = 100 \text{ mm}$
 $b = 20 \text{ mm}$ diametro puleggia = 300 mm (d_p)
 $c = 30 \text{ mm}$ $F = 500 \text{ N}$
 $d = 200 \text{ mm}$



$$\checkmark R_{Ax} = 0 \quad \sum F_x = 0$$

$$\checkmark \sum M_x = 0$$

$$T \frac{d_p}{2} - Fd = 0$$

$$T = Fd \frac{2}{d_p} = 500 \text{ N} \cdot 200 \text{ mm} \frac{2}{300 \text{ mm}}$$

$$= 666,7 \text{ N}$$

$$\checkmark \sum M_y(A) = 0$$

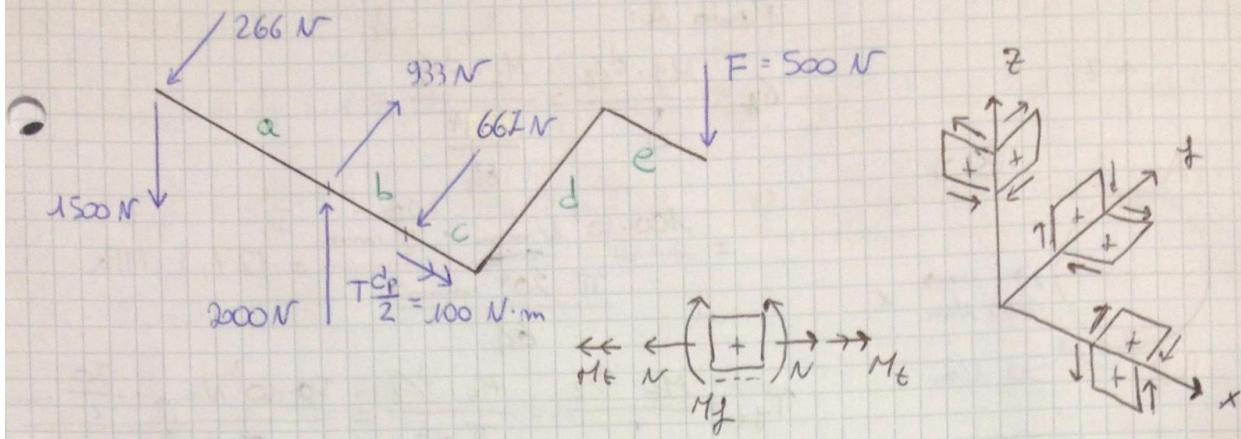
$$R_{Bz} \cdot a - F(a+b+c+e) = 0 \quad R_{Bz} = F \frac{a+b+c+e}{a} = 2000 \text{ N}$$

$$\checkmark \sum F_y = 0 \quad R_{Az} + R_{Bz} - F = 0 \quad R_{Az} = F - R_{Bz} = -1500 \text{ N}$$

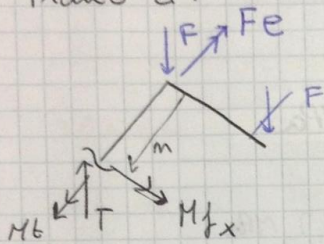
$$\checkmark \sum M_z(A) = 0$$

$$R_{By} \cdot a + T(a+b) = 0 \quad R_{By} = -T \frac{a+b}{a} = -933,38 \text{ N}$$

$$R_{Ay} + R_{By} + T = 0 \quad R_{Ay} = -R_{By} - T = 266,68 \text{ N}$$

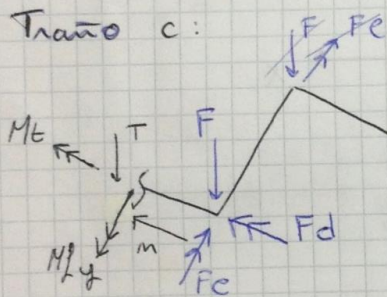


Tramo d:



$$T = F \quad M_t = F_e \quad M_{fx} = F_m$$

Tramo c:

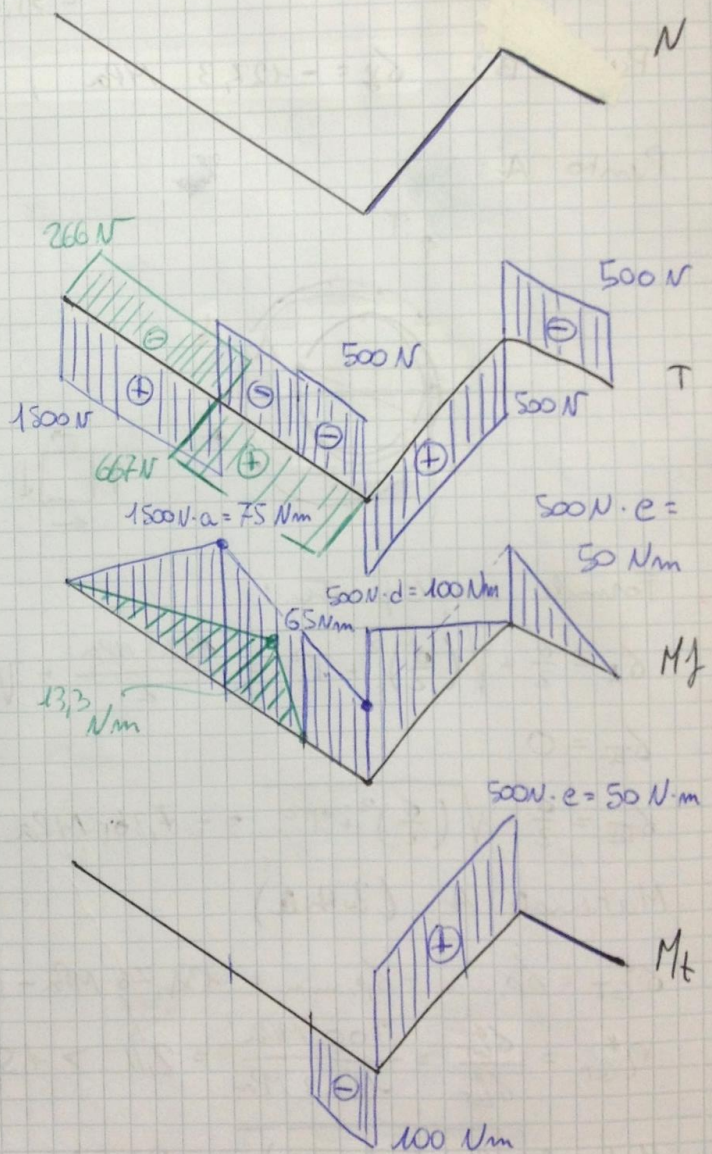


$$T = -F; \quad M_t = -F_d$$

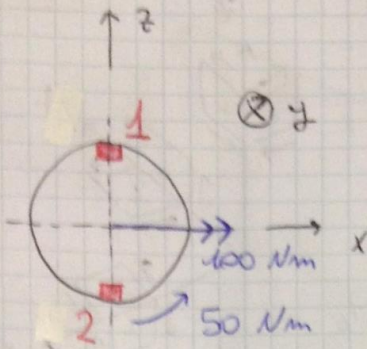
$$M_{fy} - F_e - F_m = 0 \quad M_{fy} = +F_e + F_m$$

$$M_{fy}(m=c) = 65\text{ N}\cdot\text{m}$$

Tramo a: si traciamo i pezzi a mano!



Sezione H-H:

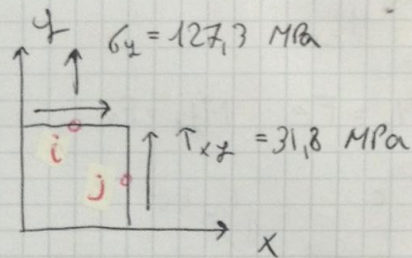
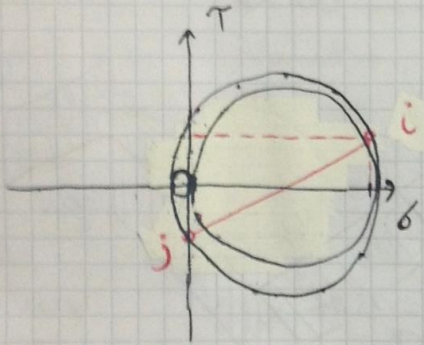


Punto A:

$$\sigma_y = \frac{M_f \cdot d/2}{J} = \frac{M_f \cdot d/2}{\frac{\pi d^4}{64}} = \frac{100 \cdot 10^3 \text{ Nmm} \cdot \frac{20}{2} \text{ mm}}{\frac{\pi \cdot 20^4 \text{ mm}^4}{64}} = 127,3 \text{ MPa}$$

$$\tau_{yz} = \frac{M_t \cdot d/2}{J_p} = \frac{M_t \cdot d/2}{\frac{\pi d^4}{32}} = \frac{50 \cdot 10^3 \text{ Nmm} \cdot \frac{20}{2} \text{ mm}}{\frac{\pi \cdot 20^4 \text{ mm}^4}{32}} = 31,8 \text{ MPa}$$

Punto 1:



Formule semplificate:

$$\sigma_I = \frac{\sigma}{2} + \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2} = \frac{127,3 \text{ MPa}}{2} + \sqrt{\left(\frac{127,3}{2}\right)^2 + 31,8^2} = 134,76 \text{ MPa}$$

$$\sigma_{II} = 0$$

$$\sigma_{III} = \frac{\sigma}{2} - \sqrt{\left(\frac{\sigma}{2}\right)^2 + \tau^2} = -7,36 \text{ MPa}$$

Materiale A: (duttile)

$$\sigma_{GT}^* = \sigma_{p,max} - \sigma_{p,min} = 134,76 \text{ MPa} - (-7,36 \text{ MPa}) = 142,13 \text{ MPa}$$

$$\eta_{GT} = \frac{R_s}{\sigma_{GT}^*} = \frac{300 \text{ MPa}}{142,13 \text{ MPa}} = 2,11 > 1,5 \text{ ok!}$$

$$\sigma_{VM}^* = \sqrt{\sigma_I^2 + \sigma_{II}^2 - \sigma_I \sigma_{II}} = 138,59 \quad \eta_{VM} = \frac{R_s}{\sigma_{VM}^*} = 2,16 \text{ ok!}$$

Materiale 2 (fragile)

$$\sigma_{GRV}^+ = \sigma_I = 134,76 \leq \frac{R_{m,t}}{\eta} \quad \eta = \frac{R_{m,t}}{\sigma_{GRV}^+} = 5,2 > 3 \text{ ok!}$$

$$\sigma_{GRV}^- = \sigma_{III} = -7,36 \text{ MPa} \geq \frac{R_{m,c}}{\eta} \quad \eta = \frac{R_{m,c}}{\sigma_{GRV}^-} = 95 > 3 \text{ ok!}$$

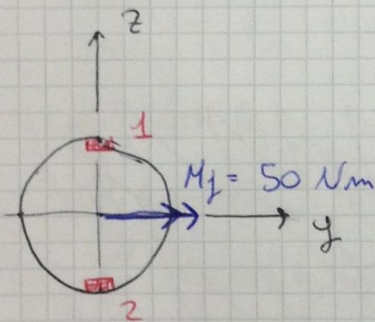
Punto 2:

$$\sigma_x = -127,3 \text{ MPa} ; \tau_{yx} = 31,8 \text{ MPa}$$

$$\sigma_I = 7,5 \text{ MPa} ; \sigma_{II} = 0 ; \sigma_{III} = -134,8 \text{ MPa} \quad \eta_c = \frac{R_{m,c}}{\sigma_{GRV}^-} = \frac{700 \text{ MPa}}{134,8 \text{ MPa}} = 5,2$$

Sezione K-K

Tabella : $\left. \begin{array}{l} D/d = 1,25 \\ r/d = 0,31 \end{array} \right\} \rightarrow K_t(M\pm) = 1,3$



Punto 1:

$$\sigma_x = \frac{M_t \cdot d/2}{\frac{\pi d^4}{64}} = \frac{M_t \cdot \frac{16 \text{ mm}}{2}}{\frac{\pi 16^4 \text{ mm}^4}{64}} = 124,34 \text{ MPa}$$

Materiale duttile:

$$\sigma_{x,max} = \sigma_x \cdot K_t = 161,6 \text{ MPa}$$

$$\sigma_{GT}^+ = \sigma_{GT}^- = 161,6 \text{ MPa} \leq \frac{R_s}{\eta} \quad \eta = \frac{R_s}{\sigma_{GT}^+} = 1,86 > 1,5 \text{ ok!}$$

Materiale fragile:

$$\sigma_{GRV}^+ = \sigma_I = 161,6 \leq \frac{R_{m,t}}{\eta} \quad \eta = \frac{R_{m,t}}{\sigma_{GRV}^+} = 4,33 > 3 \text{ ok!}$$